

DTU



HighNESS International School on Thermal Neutron Scattering Kernel Generation

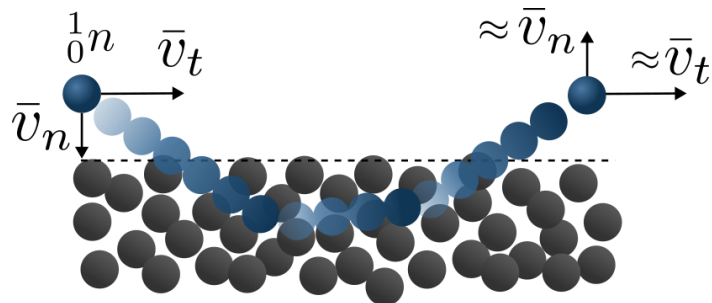
SANS plug-in for Nanodiamonds

Nicola Rizzi

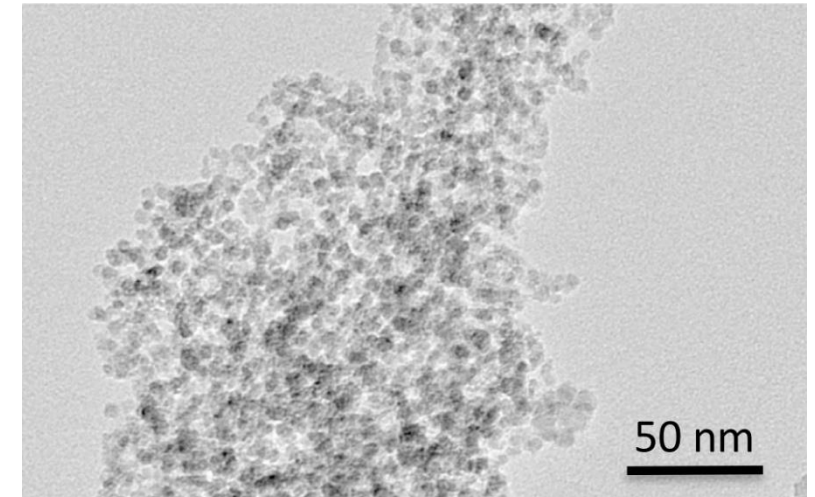
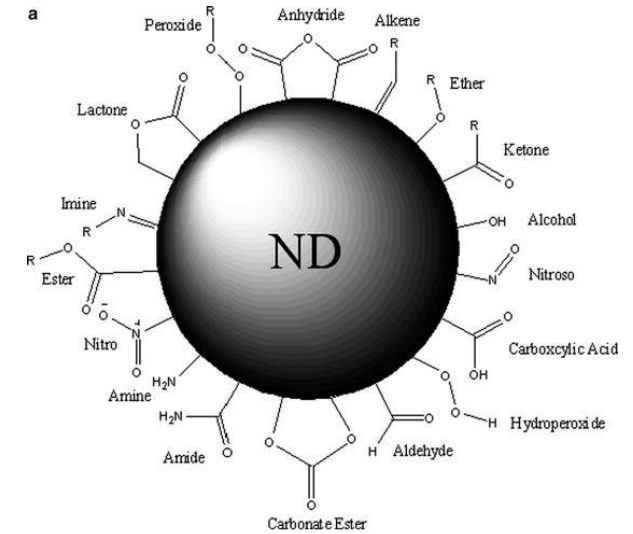
Ph.D. student

What are nanodiamond particles?

- A **diamond core** within an onion-like shell measuring few nanometers;
- The outer surface is a shell with complex chemical composition, consisting of impurities such as carbon, oxygen, nitrogen and **hydrogen**;
- Nanodiamond Powder samples showed efficient **reflector** properties for very cold neutrons (VCN) up to 10^{-4} eV [2];
- Large cross-section for small-angle elastic scattering in the VCN wavelength, and very low absorption.



Images from [5]



Main reference

NUCLEAR SCIENCE AND ENGINEERING

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Benchmarking of the NCrystal SANS Plugin for Nanodiamonds

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SANSND plugin for NCrystal

SANS experimental $I(q)$ in absolute units = $\frac{d\sigma}{d\Omega}(q)$ microscopic differential per-atom cross section with units barn sr⁻¹

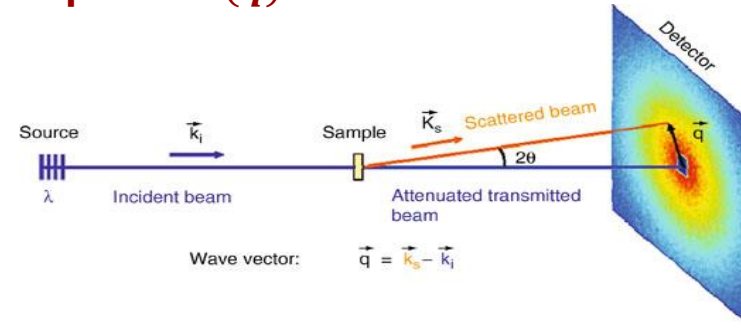
$$\sigma_{SANS}(k_0) = \int I(q) d\Omega = \int_0^{2\pi} d\phi \int_0^\pi I(q) d\theta$$

$$q = 2k_0 \sin \frac{\theta}{2} \quad \longrightarrow \quad qdq = k_0^2 \sin \theta d\theta$$

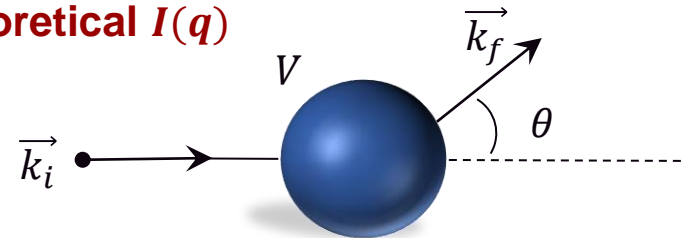
$$\sigma_{SANS}(k_0) = \frac{2\pi}{k_0^2} \int_0^{2k_0} I(q) q dq$$

total microscopic per-atom cross section

Empirical $I(q)$



Theoretical $I(q)$



Empirical models

- Piece-wise power law

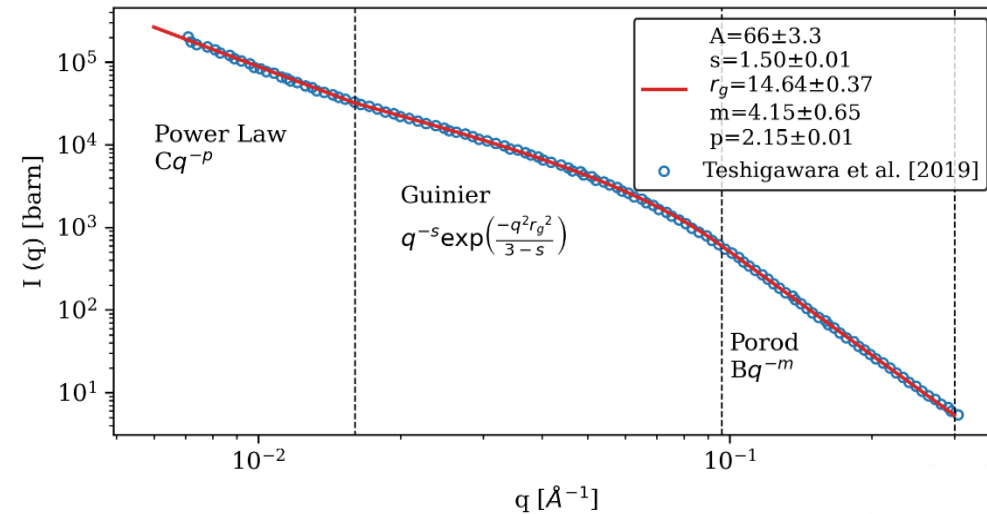
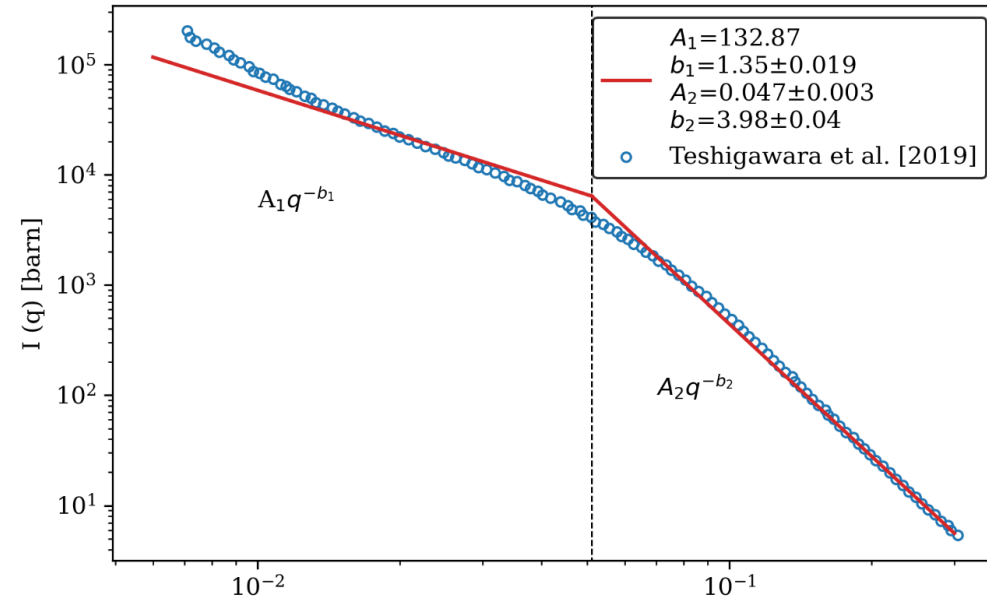
$$I(q) = \begin{cases} A_1 q^{b_1} & q < Q_0 \\ A_2 q^{b_2} & q > Q_0 \end{cases}$$

- Guinier-Porod + power law

$$I(q) = \begin{cases} Cq^{-p}, & Q_{min} \leq q \leq Q_1 \\ q^{-s} e^{\frac{-q^2 r_g^2}{3-s}}, & Q_1 < q < Q_2 \\ Bq^{-m} & q \geq Q_2 \end{cases}$$

- Data file

Data from [1]



Theoretical model

Scattering amplitude per nanoparticle for hard sphere model using first Born approximation [8]:

$$f(\theta) = -\frac{2m}{\hbar^2} V R^3 \frac{1}{(qR)} \left(\frac{\sin(qR)}{(qR)^2} - \frac{\cos(qR)}{qR} \right)$$

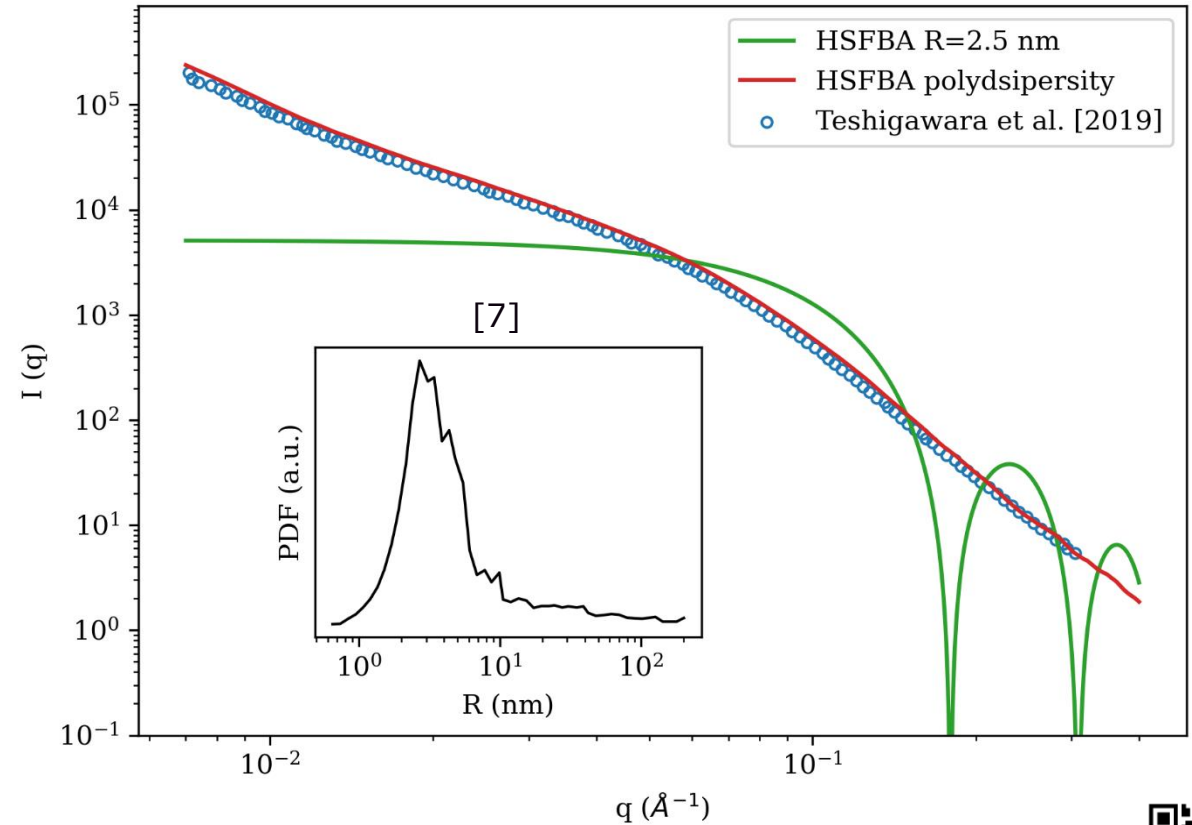
Fermi Potential

ND radius

Then $I(q)$ is just:

$$I(q) = \frac{|f(\theta)|^2}{N_c}$$

No. of C in ND



How to enable it?

<https://github.com/highness-eu/ncplugin-SANSND>

The plugin comes with a
SANSND_nanodiamond.ncmat file:

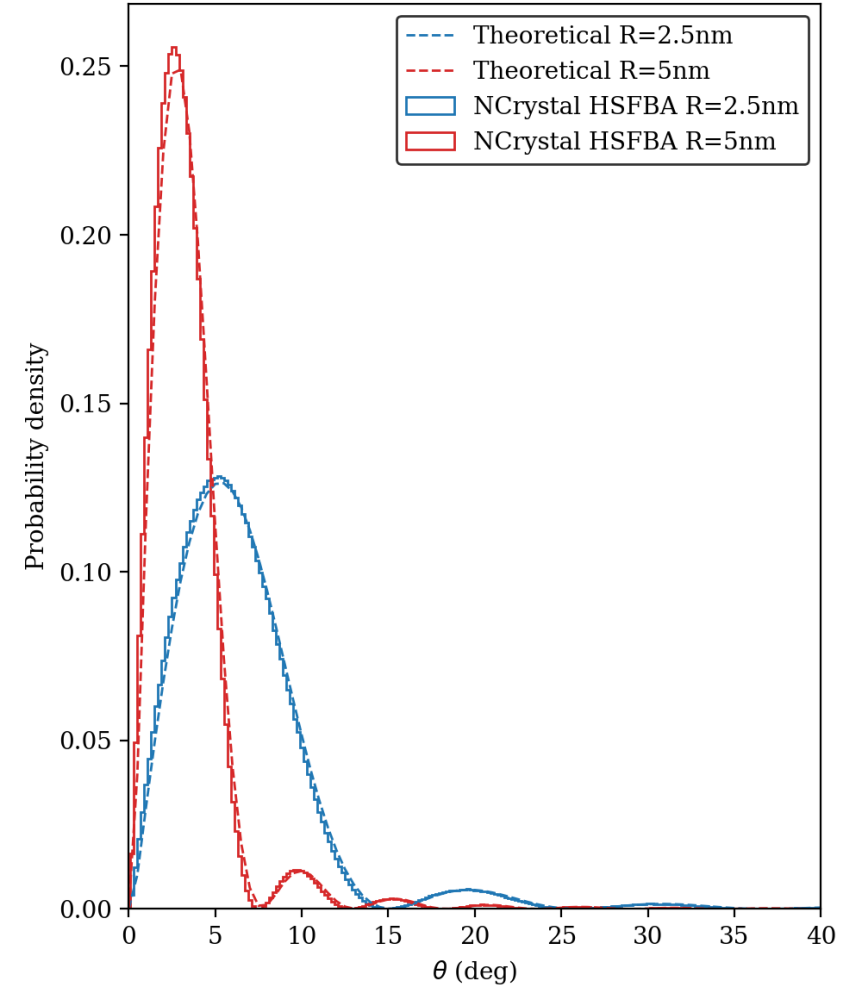
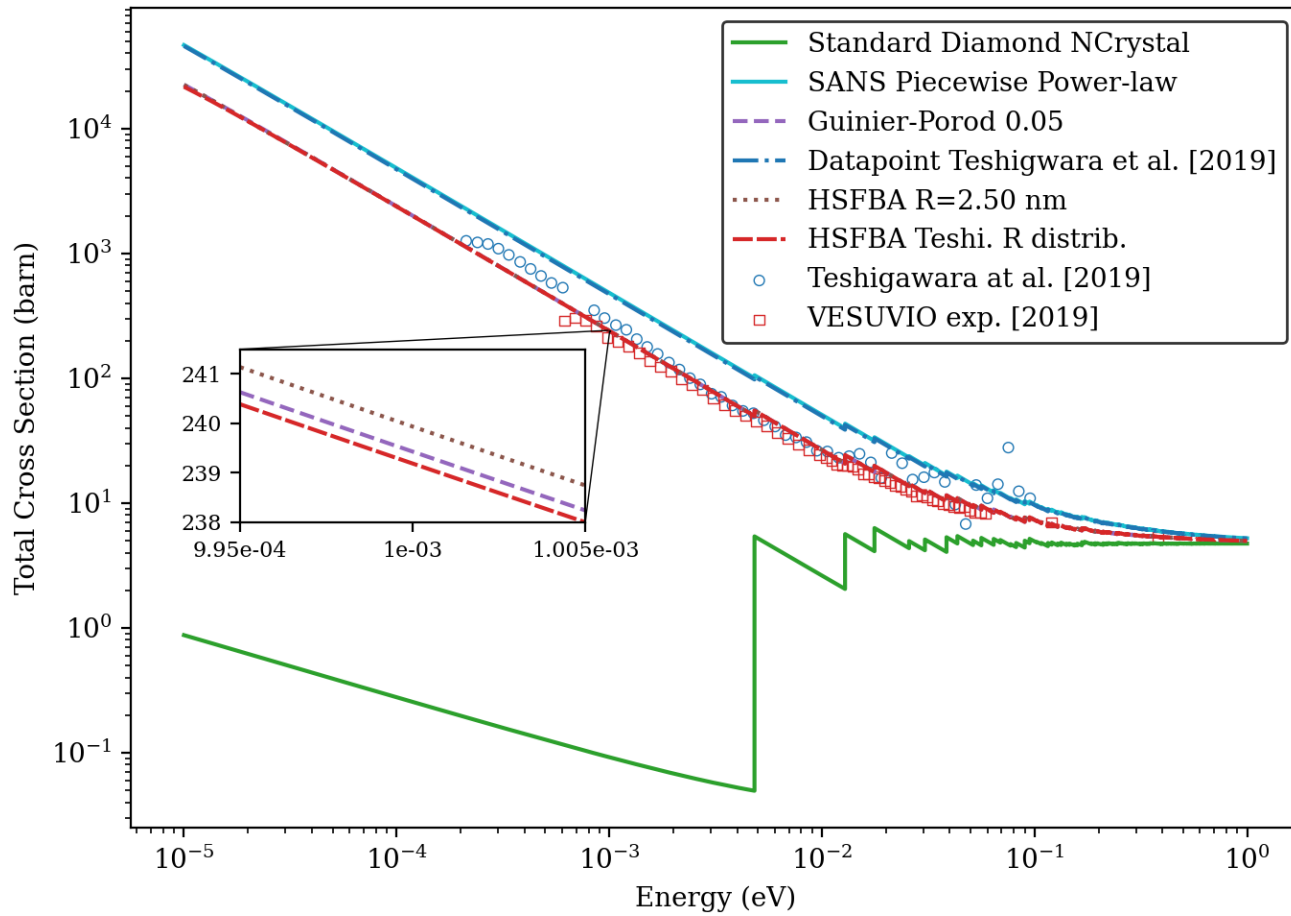
- set the right density;
- choose the model;
- pass the right parameters

```
@CUSTOM_SANSND
# custom physics that enables SANS for Nanodiamond particles
2.0 # plugin version
model # model string input (see Plugin Readme)
parameters # relevant parameters (see Plugin Readme)
```

Model	Inupt name	Input parameters
Piece-wise power law	PPF	$A_1 b_1 A_2 b_2 Q_0$
Guinier-Porod + power law	GPF	$A s r_g m p Q_{min}$
Input data file	FILE	filename
Hard Sphere First Born Approximation	HSFBA	R in nm or R distribution filename



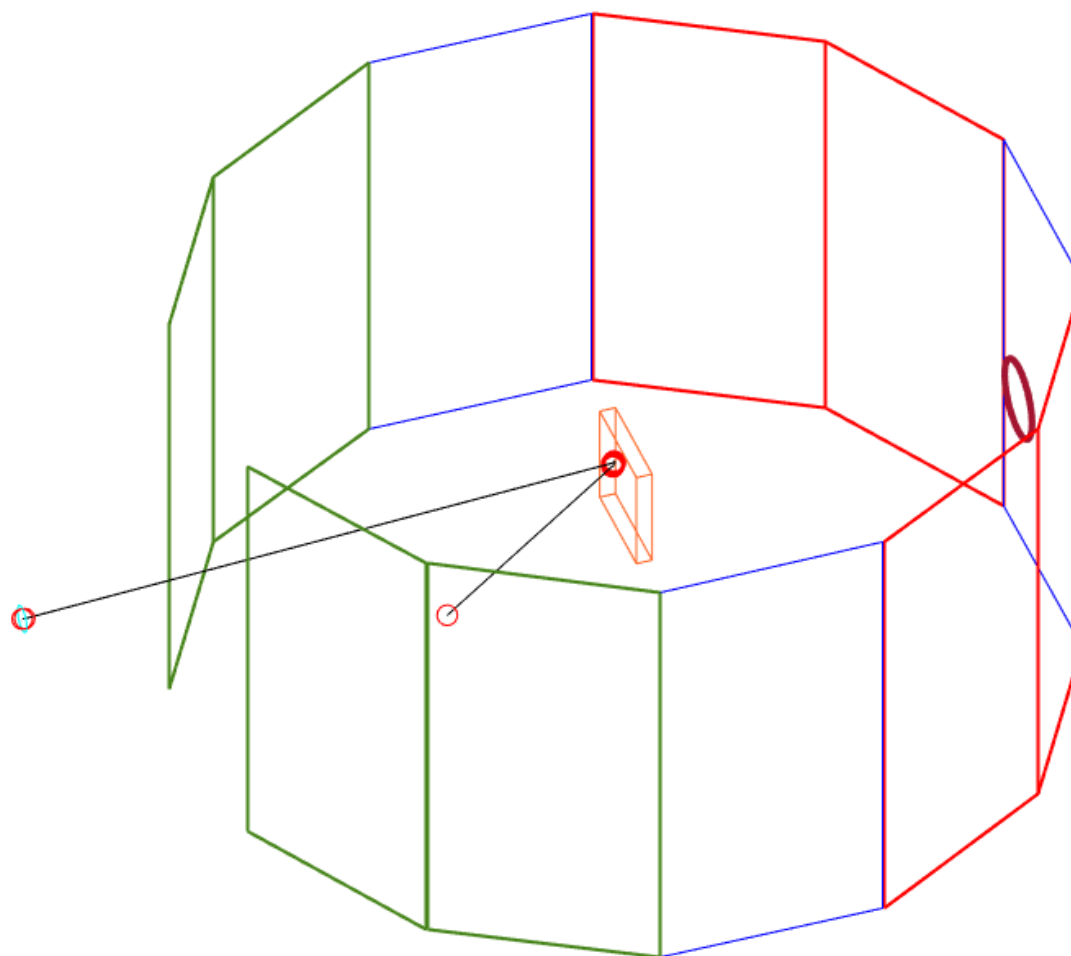
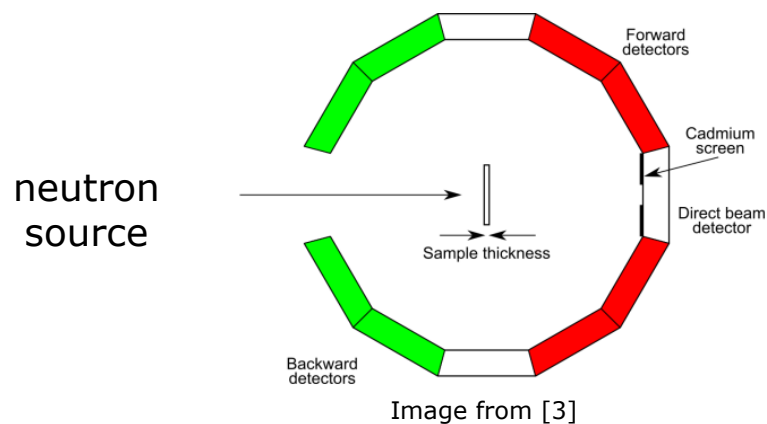
Benchmark



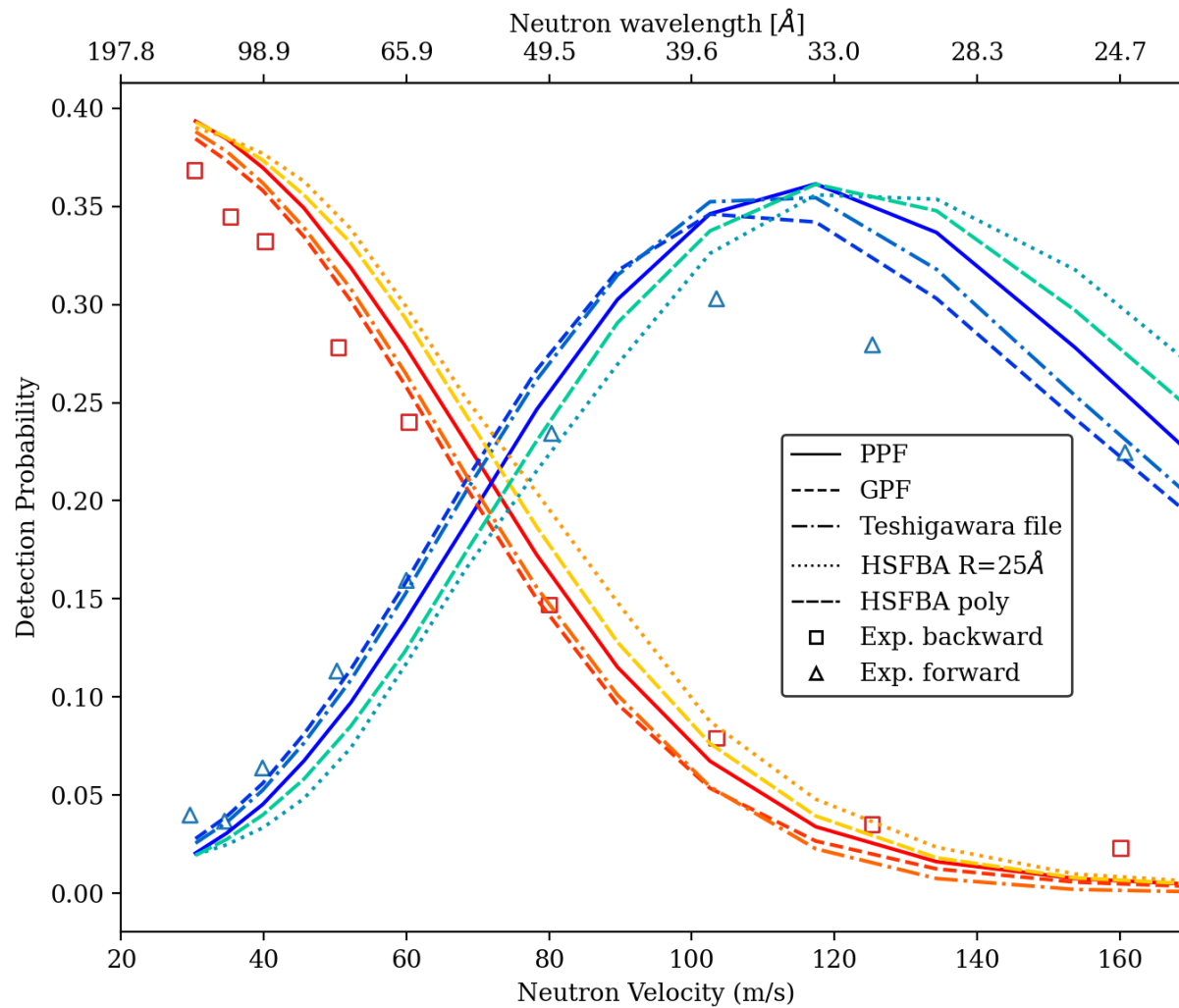
Nesvizhevsky backward reflection experiment [2]

- Nanodiamond powder sample of $4 \times 4 \text{ cm}^2$
- 0.4mm and 6mm thickness
- Monochromatic VCN-CN source
- Simple counting monitors
- Cadmium Beamstop

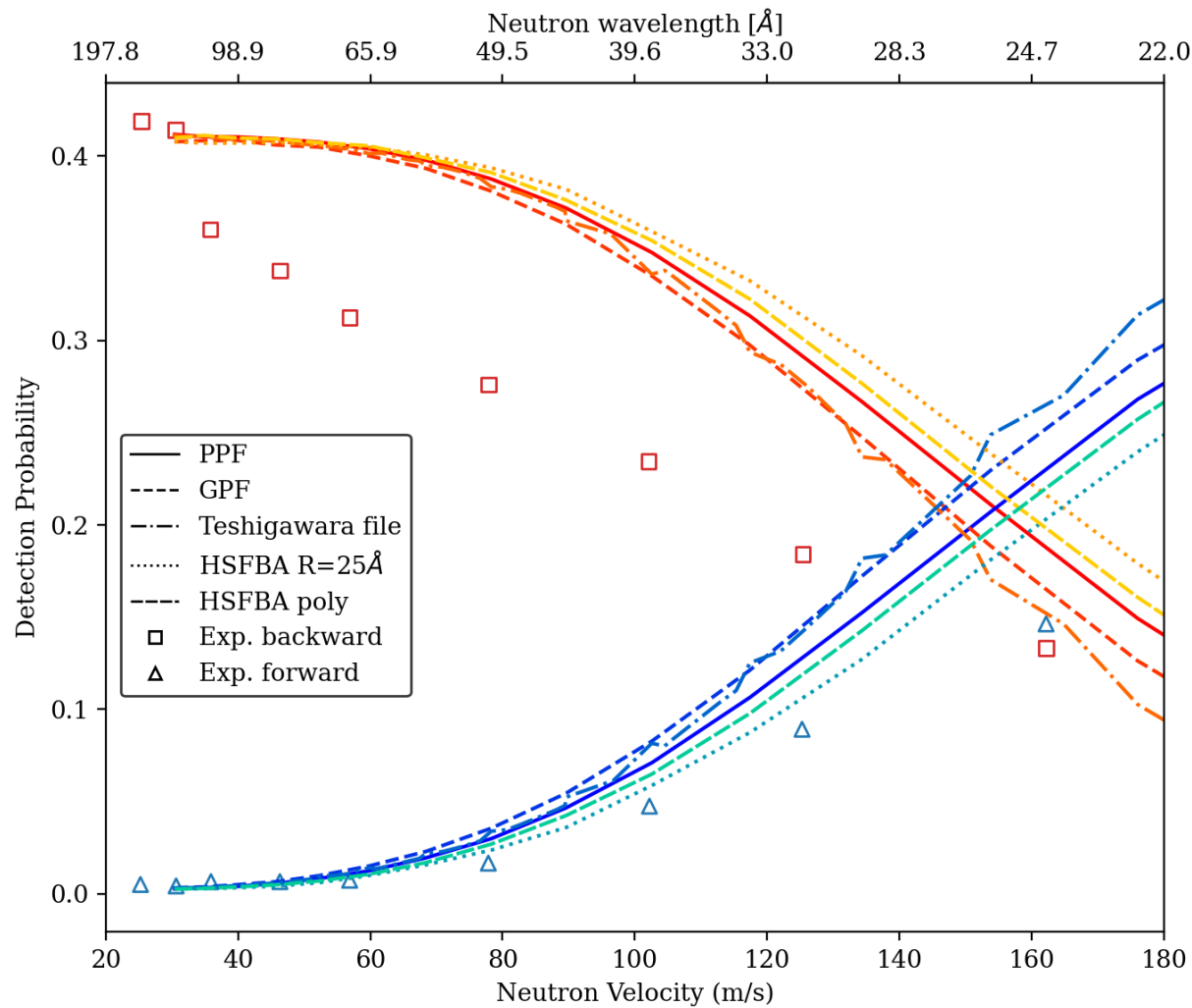
$$R = \frac{\text{Backward counts}}{\text{Forward counts} + \text{Backward counts}}$$



Benchmark on 0.4 mm sample



Benchmark on 6 mm sample



Low-angle reflectometry benchmark

- Comparison with study about Nanodiamond quasispecular reflection of cold neutrons: Nesvizhevsky et al. (2018) [4]
- Goal: test the plugin in more complex configurations where angular distribution of reflected neutrons is essential.

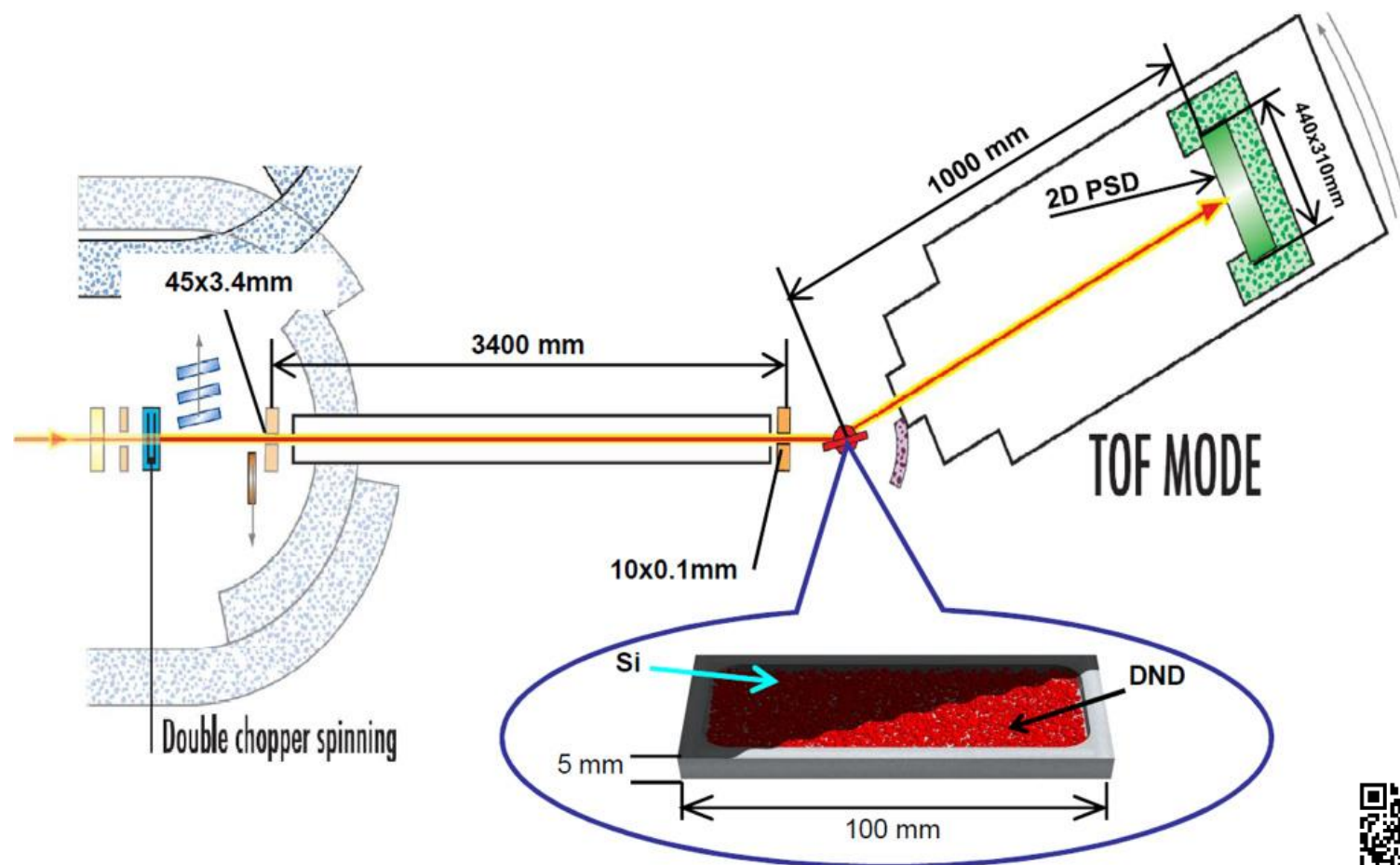
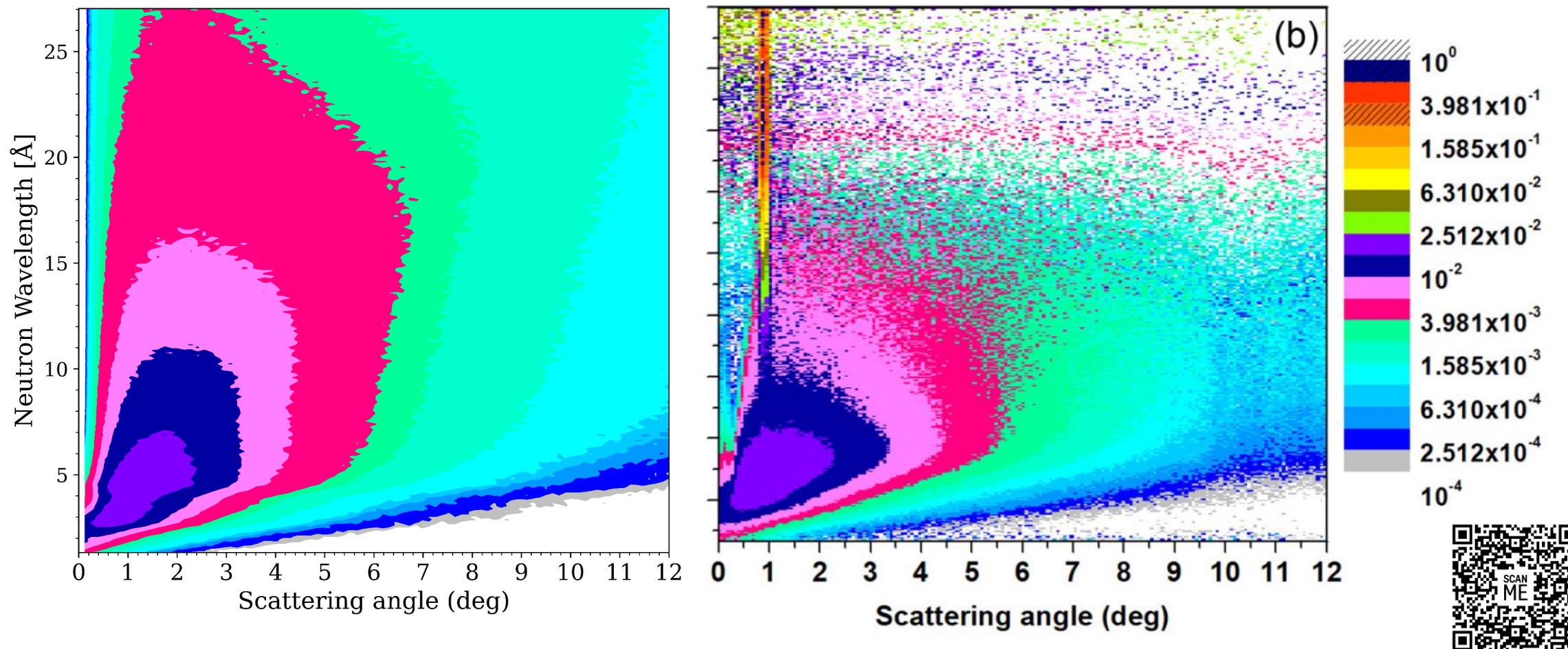


Fig. 1 from [4]



Probability of scattering

Fig. 2b from [4]



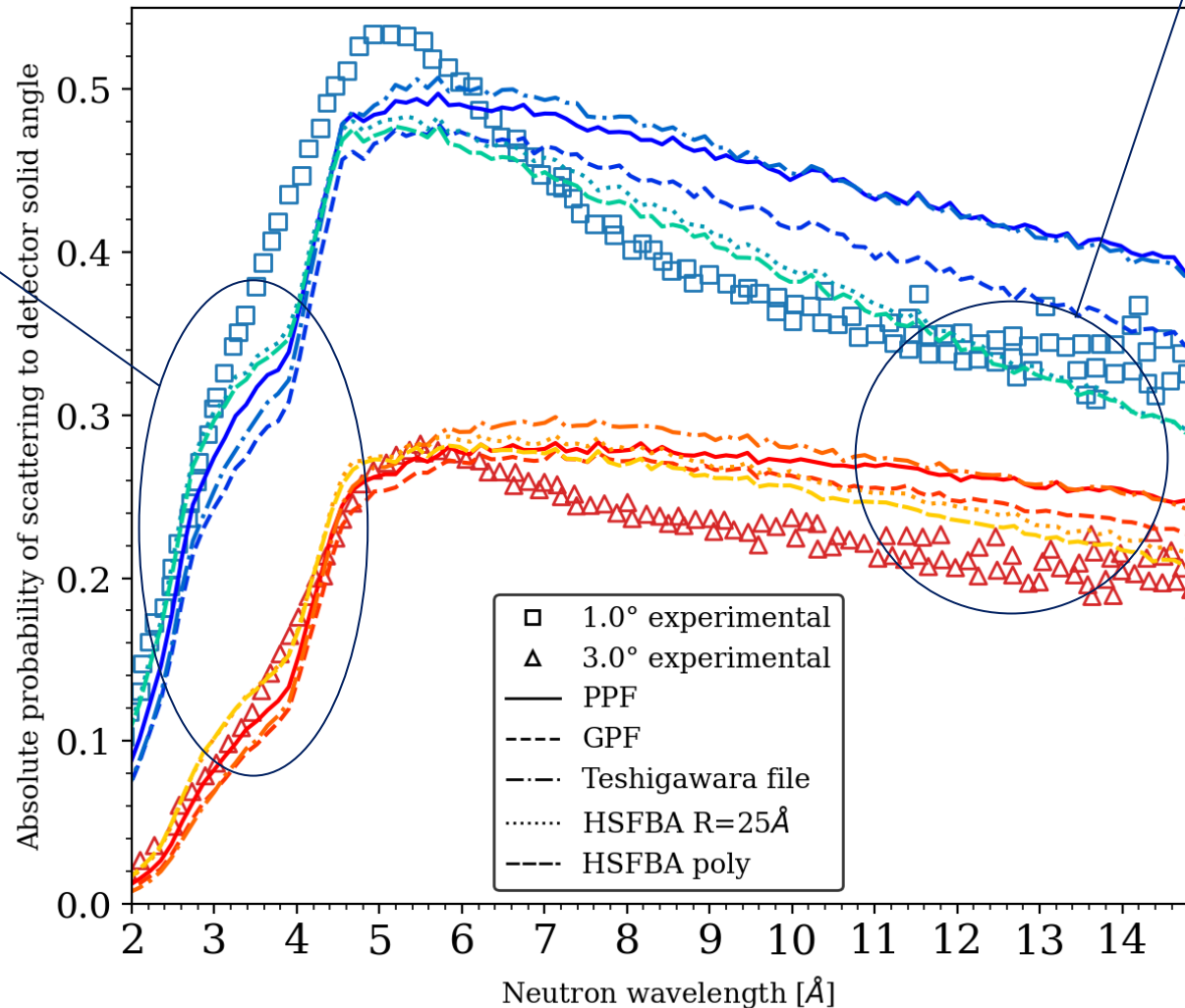
Reflection probability in λ

Decrease due to finite vertical size of the detector

Quasi-specular reflection suppressed due to:

- Diffraction on the crystal lattice of the diamond core at 3.57\AA ;
- Too small scattering angles at individual ND at wavelengths of $\sim 3\text{\AA}$ and below;

Cutoffs are not sharp due to the finite size of nanoparticles



Conclusions

- We added nanodiamond SANS scattering process to NCrystal
- Both empirical and theoretical models available
- Several ND properties in reflection of VCN well captured by our approach
- Impurities not taken into account, so just ideal ND
- We are working on further benchmarking the plugin for the enhancement of neutron extraction from Compact Accelerator-based Neutron Source and general directional extraction



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