

# Liouvillean Injection for ESSnuSB

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# Background





- Exploring options for a future multi-megawatt facility on a 20year time-scale
- Include ideas that could be feasible with advances in technology
- Gain benefit from the developments at future facilities overseas, particularly in China (C-ADSR, C-HIAF, C-SNS)



- FFAG pumplet lattices
  - scaling and non-scaling
- RCS FFAG pumplet models
- Racetrack lattices
- DF-spiral models

- Designs for
  - main ring with radius of 52m, 31m, 26m, 25m
  - test ring with radius of 2.6m, 5m



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All models have direct proton injection for a multi-megawatt beam production





**KURRI** Collaboration



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### **ESSnuSB**

Proposal to add a neutrino facility to the ESS linac



ESS linac output parameters:

Beam energy	2.0	GeV
Pulse beam current	62.5	mA
Pulse duration	2.86	ms
Pulse repetition rate	14	Hz
Beam power	5	MW

#### Proposed Ring parameters:

Beam energy	2.0	$\mathrm{GeV}$
Accumulated beam power	5	MW
Ring circumference/radius	376/60	m



### **Parameters ESSnuSB**

#### **Injection Parameters**

Accumulated beam power (MW)	5.00
Kinetic energy at injection (MeV)	2000.0
eta	0.9476
$\gamma$	3.1316
$eta \gamma$	2.9676
Linac beam current (mA)	62.50
Linac chopping factor	1.00
Repetition rate (Hz)	14.0
Total number of particles $(\times 10^{14})$	11.146
Injection interval required, $Ne/I$ (ms)	2.86
Revolution period at injection, $t \ (\mu s)$	1.32
Ring circumference (m)	375.73
Number of injected turns	2160

Single	ring	s or
4 ri	ngs	with
$2.78 \times$	$10^{14} p$	rotons
in each	•	



## **Beam Accumulation**

"The multiturn injection method by proton beam has been almost abandoned for injection from a linac to an RCS, due to its poor injection efficiency. *H-minus stripping injection is a must* to obtain highly accumulated protons in rings by hundreds of turns."

Reviews of Accelerator Science and Technology Volume 6: Accelerators for High Intensity Beams, April 2014

### Downside

- Complicated injection chicane
- Needs a mechanism for handling unstripped H<sup>-</sup> and partially stripped H<sup>0</sup> excited states
- Dealing with stripped electrons
- Foil heating, foil lifetime issues, nuclear scattering, multiple scattering, foil traversals, foil replacement system
- Intra-beam stripping in linac and injection line
- These are all causes of beam loss





# H<sup>-</sup> Injection Regions





- J-Parc and SNS injection layouts.
- H and V bump magnets to paint the beam and reduce foil traversals.
- Can also use dispersion painting, injecting in a dipole.

## **Non-Liouvillean Injection**



Optimising the closed orbit bumps to minimise the number of foil traversals is very like optimising to avoid beam loss for a Liouvillean system

H- injection modelling for a possible new 16 GeV booster ring for Fermilab (FNAL Driver Report, 2000)



# **Direct Multiturn Injection**

- Conventional method is to inject into one plane (h) and fill the other (v).
  Then (in some cases) rotate phase planes and repeat.
- Phase space has to be conserved (Liouville)



Optimised 6-turn injection scheme, Q=0.391 (C.Prior, 1980)



5-turn injection with Q=0.25: less than 5/9 of phase space occupied by beam, dilution F>9/5=1.8

### Optimised schemes from 1980 study

Number	Dilution
of turns	F
6	1.56
7	1.92
8	1.86
9	2.01
10	2.15

Expected number of injection turns  $N \approx \frac{1}{F} \frac{\epsilon_{\text{ring}}}{\epsilon_{\text{inj}}}$ 

where F is the phase space dilution factor

# **Multiturn Injection of Protons**

- Liouvillean injection using a tilted electrostatic septum
- Simple injection chicane
- Injection simultaneously into 4D transverse phase space
- Optimise *h* and *v* closed orbit bumps to minimise beam loss
- Requires careful choice of septum angle  $\theta$  and ring optics (tunes,  $\beta$ -functions at injection point).



• Earlier simulations for HIDIF suggest maximum number of turns is

$$N_{\rm max} \approx \frac{1}{F} \frac{(\epsilon_h \epsilon_v)_{\rm ring}}{(\epsilon_h \epsilon_v)_{\rm inj}} \qquad \text{where} \qquad F \approx 20$$



### HIDIF Project 1996-2000



# **2-Plane Liouvillean Injection**

- Obeys Liouville's theorem, preserving volumes in phase space.
- Tilted electrostatic septum at angle  $\theta$
- Orbit bumps in transverse plane to avoid beam loss at septum
- Correlated painting
- HIDIF: 20 turns, ε<sub>inj</sub>=4 into ε<sub>ring</sub>=40 (mm.mrad)



Injection scheme for HIDIF, 1998, (Bi+1)

## **Chinese HIAF**



### **MIS-codes**

- MIS=Multi-turn Injection Scheme
- No space charge, geometric problem
- Requires only knowledge of optical parameters at injection point.
- MISHIF main code
  - optimises  $\theta$ , finds closed orbit variation over injection cycle, also suggests improved ring parameters
  - minimises phase space volume that falls on wrong side of septum
- MISOPT refined optimisation
  - based on Harwell subroutines
  - Alternative MISPRAX uses new version of old praxis routine
- MISPLOT graphical output
  - -generates particles to fit optimised scheme; standard matrix transport
  - -able to identify beam loss
- MISTRACK, MISKVBL
  - generate relevant parts of input datasets for lattice code and 2D(transverse) tracking code Track2D.

### **Preferred Conditions for Injection**

Two conditions desirable to minimise phase space wastage:

(i) 
$$\frac{\beta}{\beta_i} \le \left(\frac{\epsilon}{\epsilon_i}\right)^{\frac{1}{3}}$$

(ii) 
$$\frac{\alpha_i}{\beta_i} = \frac{\alpha}{\beta} = -\frac{x'_i - x'_o}{x_i - x_o}$$

- where subscripts *i* and *o* refer to the injected turn and the closed orbit respectively.
- MIS-codes incorporate these by default (can be switched off)
- Codes also include option on painted distribution (e.g. as uniform as possible)





2. Condition 
$$\frac{\alpha_i}{\beta_i} = \frac{\alpha}{\beta}$$
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places the turn on axis and  
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4. Condition  $\frac{\beta}{\beta_i} \leq \left(\frac{\epsilon}{\epsilon_i}\right)^{\frac{1}{3}}$  matches the curvatures to minimise wasted phase space

## Implications for ESSnuSB

### **Injection Parameters**

Kinetic energy at injection (MeV)	2000.0
Linac proton beam current (mA)	62.50
Linac $1\sigma$ normalised emittance ( $\pi$ mm.mrad)	0.25
Unnormalised $(3\sigma)$ injected emittances $(\pi \text{ mm.mrad})$	0.76
Painted emittances of ring beam ( $\pi$ mm.mrad)	100.00
Expected tune depression	0.025
Number of particles $N$ (×10 <sup>14</sup> )	2.82
Linac chopping factor	1.00
Bunching factor during injection	1.00
Injection interval, $Ne/I$ (µs)	723.62
Revolution period at injection, $t \ (\mu s)$	1.32
Mean radius at injection energy, $\beta ct/2\pi$ (m)	59.80
Number of injected turns	547

Assumes 4 rings and accumulates a total of  $5.05\,\mathrm{MW}$  beam power,  $1.26\,\mathrm{MW}$  in each ring.

$$\Delta Q_v = -\frac{Nr_p}{\pi\epsilon_v \left(1 + \sqrt{\epsilon_h/\epsilon_v}\right)\beta^2 \gamma^3} \frac{1}{B_f}$$



## **Example Ring**



• Base tunes: 
$$Q_x = 8.678324, Q_y = 8.706738$$



### **Preferred Conditions**

$$\frac{\beta}{\beta_i} \le \left(\frac{\epsilon}{\epsilon_i}\right)^{\frac{1}{3}} = 5.0903 \qquad \Longrightarrow \qquad \begin{cases} \beta_{ix} \ge 1.0899\\ \beta_{iy} \ge 1.1135 \end{cases}$$

$$\frac{x_i' - x_o'}{x_i - x_o} = -\frac{x_o'}{x_i - x_o} = -\frac{\alpha_x}{\beta_x} = 0.10554 = -\frac{\alpha_{ix}}{\beta_{ix}}$$
$$u_i' - u_i' \qquad u_i' \qquad \alpha_u$$

$$\frac{y_i - y_o}{y_i - y_o} = -\frac{y_o}{y_i - y_o} = -\frac{\alpha_y}{\beta_y} = -0.10487 = -\frac{\alpha_{iy}}{\beta_{iy}}$$

Optimised values from code for 500 turns:

- Machine tunes:  $Q_x = 8.7436, Q_y = 8.8030$  $Q_x = 8.6783, Q_y = 8.7067$
- Septum angle:  $\theta = 44.75^{\circ}$
- Injected turns:  $\beta_{ix} = 1.3984, \alpha_{ix} = -0.1476, \beta_{iy} = 1.3092, \alpha_{iy} = 0.1373$
- Injected emittances:  $\epsilon_{ix} = \epsilon_{iy} = 0.758 \,\pi \,\mathrm{mm.mrad}$

### First results - 500 turns

REV	CLOSEI	ORBIT	INJECTE	ED BEAM	MACHINE PARAMETERS			BEAM EMITTANCES		
	x	y	x	y	$eta_x$	$eta_{m{y}}$	$lpha_x$	$lpha_y$	$\epsilon_x$	$\epsilon_y$
1	27.2277	28.3963	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	13.8594	11.5512
60	23.6765	24.1538	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	26.5669	25.4612
120	22.5140	19.9114	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	31.7811	46.0798
180	20.0726	18.4127	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	44.4254	54.9670
240	17.6969	17.3540	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	58.8854	61.7499
300	15.1290	16.9142	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	76.8061	64.6874
360	12.8864	16.4160	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	94.4013	68.0972
420	12.2175	14.6556	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	100.0001	80.8479
450	12.2175	13.4570	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	100.0001	90.1548
500	12.2175	12.2547	34.7475	35.0714	5.5480	5.6681	-0.5855	0.5944	100.0001	100.0001

Total beam loss =0.658 % (assuming uniform beam)

EQUATION OF SEPTUM ax + by + c = 0, with a = 0.704055, b = 0.710146, c = -47.362466 (x and y in mm)

- Apart from closed orbit bumps, all parameters constant during injection
- Space charge forces omitted













PARTICLES REMAINING PER INJECTED TURN





## **Conclusion 1**

- 500 turns with zero beam loss looks possible
- However, ring emittance of 100  $\pi$  mm.mrad looks small. Cf. 300  $\pi$  mm.mrad for SNS and ~400  $\pi$  mm.mrad in ISIS
- Higher current proton sources are readily available (up to ~200 mA)
- So what could we do with 100 mA and 300  $\pi$  mm.mrad?

Injection Parameters for  $100\,\mathrm{mA}$ 

Accumulated beam power (MW)	5.00
Linac beam current (mA)	100.00
Repetition rate $(Hz)$	14.0
Total number of particles $(\times 10^{14})$	11.146
Injection interval required, $Ne/I$ (ms)	1.79
Revolution period at injection, $t \ (\mu s)$	1.32
Ring circumference (m)	375.73
Number of injected turns	1350



# 1500 Turn Model (5.55 MW)

REV	CLOSED ORBIT INJECTED BEAM			MACHINE PARAMETERS				BEAM EMITTANCES		
	x	y	x	y	$eta_x$	$eta_{m{y}}$	$lpha_x$	$lpha_{m{y}}$	$\epsilon_x$	$\epsilon_y$
1	37.2083	37.6036	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	51.7754	49.2979
150	30.4583	34.8917	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	101.1682	66.3779
300	26.9703	30.6787	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	133.1499	98.2712
450	23.0223	28.6189	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	174.6423	116.1733
600	19.7906	27.0791	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	212.7880	130.5333
750	18.2672	24.5290	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	232.0749	156.1565
900	18.2672	20.6426	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	232.0749	199.6189
1050	18.2672	16.9552	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	232.0749	245.7842
1200	18.2672	13.4154	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	232.0749	294.6146
1350	15.9127	13.0437	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	263.5299	299.9976
1500	13.3526	13.0437	53.1741	53.3387	5.5480	5.6681	-0.5855	0.5944	300.0000	299.9976

#### Total beam loss =0.00 % (assuming uniform beam)

EQUATION OF SEPTUM ax + by + c = 0, with

a = 0.789315, b = 0.613989, c = -72.757873 (x and y in mm)

Septum angle  $\theta = 52.12^{\circ}$ 

Ring acceptance  $\mathcal{A} = 480 \,\pi \,\mathrm{mm.mrad}$ 

Space charge tune depression  $\left(\propto \frac{N}{\epsilon}\right) = 0.033$ 



